

TRIBHUVAN UNIVERSITY
INSTITUTE OF ENGINEERING
Solution of B.E. Entrance Test (2075)
Set: II (A)

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|---------|---------|---------|---------|
| 1. (A) | 2. (B) | 3. (C) | 4. (D) |
| 5. (D) | 6. (C) | 7. (B) | 8. (A) |
| 9. (A) | 10. (A) | 11. (C) | 12. (C) |
| 13. (D) | 14. (D) | 15. (B) | |
| 16. (B) | | | |

Solution

280 ml of gas at NTP weigh 2 gm

22400 ml of gas at NTP weigh $\frac{2 \times 22400}{280} = 160$ gm

Molecular weight of the gas = 160

17. (D)

Solution: pH = - log of strong acid

$$= - \log 0.2 = 0.69$$

18. (C)

Solution:

Co -27 d-block element

19. (B)

Solution: $C_3H_8 + 5O_2 \longrightarrow 3CO_2 + 4H_2O$

44 g of Propane required 5×22.4 L

$$4.4 \text{ g Propane required } \frac{5 \times 22.4 \text{ L}}{44 \text{ L}} \times 4.4 = 11.2 \text{ L}$$

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|---------|---------|---------|---------|
| 20. (A) | 21. (A) | 22. (C) | 23. (D) |
| 24. (B) | 25. (A) | 26. (D) | |

27. (B) Two vectors of equal magnitude and directed in opposite directions give zero resultant.
28. (C) When the particle moves with uniform velocity, acceleration is zero.
29. (C) The energy transfer in vacuum is by radiation.
30. (C) Beats cannot be heard due to persistence of sound if the beat frequency is more than 10 Hz.
31. (D) The critical angle for diamond is small due to high refractive index. So large scale total internal reflection takes place.
32. (D) concave mirror produces magnified virtual image when the object is between the pole and the focus.
33. (A) The image formed in an astronomical telescope is inverted and virtual.
34. (A) The work done in taking a charge on the closed path is zero because the electric field is conservative.
35. (B) The radius of the circular path is given by $r = \frac{mv}{qB}$. As radius is directly proportional to v and hence the radius of the circle increases.

36. (B) By increasing the intensity of incident beam, the number of emitted photo-electrons can be increased. Hence number of photo-electrons emitted is proportional to the intensity of incident beams.

37. (D) 3 men and 3 women be seated in a row if two persons of the same sex do not sit together = $3!.3!.2! = 72$

38. (C) $y = \frac{2}{1-x}$
 $\frac{dy}{dx} = \frac{2}{(1-x)^2}$

$$\frac{d^2y}{dx^2} = \frac{4}{(1-x)^3}$$

At $x = -1$, $\frac{d^2y}{dx^2} = \frac{4}{(1+1)^3} = \frac{1}{2}$

39. (A) Here $a_1 = 2, a_2 = -1, a_3 = 4$ and $b_1 = -3, b_2 = 2, b_3 = 2$ and if θ is the angle then

$$\cos\theta = \frac{a_1b_1 + a_2b_2 + a_3b_3}{\sqrt{a_1^2 + a_2^2 + a_3^2}\sqrt{b_1^2 + b_2^2 + b_3^2}} = 0$$

Therefore, $\theta = \frac{\pi}{2}$.

40. (B) $\tan 3\theta = -1$

$$3\theta = -\frac{\pi}{4}$$

$$3\theta = n\pi - \frac{\pi}{4}$$

$$\theta = \frac{n\pi}{3} - \frac{\pi}{12}$$

41. (D) $f(x+2) = x^2 + 4x + 8$ \

$$f(x+2) = (x+2)^2 + 4$$

$$f(x) = (x)^2 + 4$$

$$f(-2) = (-2)^2 + 4 = 8$$

42. (D) y is negative for all x

43. (D) $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$

$$|\vec{a} + \vec{b}|^2 = |\vec{a} - \vec{b}|^2$$

$$\vec{a} \cdot \vec{b} = 0$$

$$|\vec{a}||\vec{b}|\cos\theta = 0 \quad \text{i.e. } \theta = \frac{\pi}{2}$$

44. (B) $2k - 2 = 1 - k$

$$k = 1$$

45. (B) $y = x^2 - 2x - 5$

$$x \text{ component of the stationary point} = -\frac{b}{2a} = -\frac{-2}{2 \cdot 1} = 1$$

and $y = -6$. Therefore $(1, -6)$ is the stationary point.

46. (B) If $x > 0$, $\frac{d}{dx} \log|x| = \frac{d}{dx} \log x = \frac{1}{x}$

$$\text{If } x < 0, \frac{d}{dx} \log|x| = \frac{d}{dx} \log(-x) = \frac{1}{-x} \cdot -1 = \frac{1}{x}$$

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|---------|---------|---------|---------|
| 47. (A) | 48. (A) | 49. (A) | 50. (C) |
| 51. (C) | 52. (C) | 53. (D) | 54. (A) |
| 55. (C) | 56. (B) | 57. (D) | 58. (A) |
| 59. (C) | 60. (B) | 61. (D) | 62. (A) |
| 63. (C) | 64. (B) | | |
| 65. (C) | | | |

Solution

$$V_1 S_1 \text{ (acid)} = V_2 S_2 \text{ (base)}$$

$$20 \times S_1 = 25 \times 0.1 \quad S_1 = \frac{25 \times 0.1}{20} \text{N} = 0.125 \text{ N}$$

$$S_1 = 0.125 \text{ N}$$

We know,

$$\text{gm/liter} = \text{Normality} \times \text{Equivalent weight}$$

$$7.875 = 0.125 \times \text{Equivalent weight}$$

$$\text{Equivalent weight} = 7.875 / 0.125$$

$$= 63.00$$

66. (B)

Solution:

Total quantity of electricity passed = $0.75 \times 45 \times 60 = 2025$ Coulombs
 2025 coulomb of electricity deposits 0.6662 g of metal
 96500 coulomb of electricity deposits $= \frac{0.6662}{2025} \times 96500$
 $= 31.75 \text{ g}$

67. (C) 68. (B)

69. (D) Pascal second = pressure \times time

$$= \frac{[ML T^{-2}]}{[L^2]} = [ML^{-1} T^{-1}]$$

$$\text{Further, } \eta = \frac{F}{6\pi\eta r} = \frac{[M L T^{-2}]}{[L \times L T^{-1}]} = [ML^{-1} T^{-1}]$$

70. (A) $\lambda = \frac{0.693}{T_{1/2}} = \frac{0.693}{1620 \times 365 \times 24 \times 60 \times 60}$

$$\text{And } N = \frac{6.023 \times 10^{23}}{226}$$

$$\text{We know that, } \frac{dN}{dt} = \lambda N$$

$$\therefore \frac{dN}{dt} = 3.61 \times 10^{10}$$

71. (D) we know that $E \propto \frac{1}{n^2}$

$$\therefore E_1 = \frac{-13.6}{2^2} = -3.4 \text{ eV}$$

72. (A) In case of simple harmonic motion

$$\text{K.E.} = \frac{1}{2} m R^2 \omega^2 \cos^2 \omega t$$

$$\& \text{P.E.} = \frac{1}{2} m R^2 \omega^2 \sin^2 \omega t$$

$$\text{T.E.} = \frac{1}{2} m R^2 \omega^2$$

According to the equation,

$$\frac{1}{2} m R^2 \omega^2 \cos^2 \omega t = \frac{1}{4} \frac{1}{2} m R^2 \omega^2 \Rightarrow \omega t = \pi/3$$

$$\text{Now, } x = R \sin \omega t = R \sin(\pi/3) = \frac{\sqrt{3}}{2} R$$

73. (A) $x_n = \frac{a}{2} (2n - 1) = \frac{10}{2} (2n - 1)$

$$x_n = \frac{1}{2} at^2 = 5t^2 = 45$$

$$\therefore n = 5$$

$$\text{Now, } h = \frac{1}{2} g \times 5^2 = \frac{1}{2} \times 10 \times 25 = 125 \text{ m}$$

74. (D) Here, $\frac{n_s}{n_p} = \frac{p_o}{p_i}$

$$\frac{3}{2} = \frac{p}{p_i} \Rightarrow p_i = \frac{2p}{3}$$

75. (B) $\cos \theta = \frac{B_H}{B} = \frac{3 \times 10^{-5}}{6 \times 10^{-5}} = \frac{1}{2} \quad \therefore \theta = 60^\circ$

76. (C) Hence, $\frac{1}{2} mv^2 = eV$

$$v = \sqrt{\frac{2Ve}{m}} = \sqrt{2 \times 200 \times 1.6 \times 10^{11}} = 8 \times 10^6 \text{ m/s}$$

77. (C) $\mu = \frac{1}{\sin c} \quad \sin c = \frac{3}{5}$

$$\therefore \mu = \frac{5}{3} \quad \text{Also, } \tan i_p = \mu$$

$$\therefore i_p = \tan^{-1} \left(\frac{5}{3} \right)$$

78. (D) He should use a concave lens of focal length 60cm.

$$\therefore p = -\frac{1}{0.6} = -1.66 \text{ D}$$

79. (B) $25 = \left(1 - \frac{300}{T_1} \right) 100 = \frac{100T_1 - 30000}{T_1}$

$$25 T_1 = 100T_1 - 30000$$

$$\therefore T_1 = 400 \text{ k.} = 400 - 273 = 127^\circ \text{C}$$

80. (A) $\frac{\Delta l}{l} = 0.10\% = 0.001$ & $\Delta T = 100^\circ\text{C}$

Now, $\frac{\Delta l}{l} = \alpha \Delta T$ $0.001 = \alpha \times 100 \Rightarrow \alpha = 10^{-5} / ^\circ\text{C}$

Further $\gamma = 3\alpha = 3 \times 10^{-5} / ^\circ\text{C}$

$\therefore \frac{\Delta v}{V} \times n \Delta T = 3 \times 10^{-5} \times 100 = 3 \times 10^{-3}$

or $\frac{\Delta v}{V} \times 100 = 0.30\%$

81. (A) $v \propto r^2$

Hence $5 \propto r^2$ and $v \propto R^2$

$v \propto (2^{1/3}r)^2 \propto 4^{1/3} r^2$

$\therefore \frac{v}{5} = (4)^{1/3} \Rightarrow v = 5 \times 4^{1/3} \text{ cm/s}$

82. (D) $g_h = g(1 - \frac{2h}{r})$ and $g_x = g(1 - \frac{x}{R})$

Given that $g_h = g_x$

$\therefore x = 2h$

83. (C) The acceleration a_1 without friction is

$a_1 = g \sin \theta$ --- (a)

The acceleration a_2 with friction is

$a_2 = g \sin \theta - \mu g \cos \theta$ --- (b)

Further, $t = \sqrt{\left(\frac{2s}{a}\right)}$

$\therefore \frac{t_1}{t_2} = \sqrt{\frac{a_2}{a_1}}$

$\frac{1}{2} = \sqrt{\frac{g \sin \theta - \mu g \cos \theta}{g \sin \theta}}$

$\frac{1}{2} = \sqrt{1 - \mu \tan \theta}$

$\mu \tan \theta = \frac{3}{4}$

$\mu = \frac{3}{4} \frac{1}{\tan 45^\circ} = \frac{3}{4} = 0.75$

84. (B) $|\vec{a} - \vec{b}|^2 = |\vec{a}|^2 + |\vec{b}|^2 - 2\vec{a} \cdot \vec{b}$

$= 2 - 2|\vec{a}||\vec{b}|\cos \theta$

$= 2(1 - \cos \theta)$

$= 4 \sin^2 \frac{\theta}{2}$

Therefore, $|\vec{a} - \vec{b}| = 2 \sin \frac{\theta}{2}$

85. (B) $\int (1 - \cos x + \cos^2 x - \cos^3 x + \cos^4 x - \dots) dx = \int \frac{1}{1 + \cos x} dx$
 $= \int \frac{1}{2} \sec^2 \frac{x}{2} dx$
 $= \tan \frac{x}{2} + c$

86. (C) Coefficient of x^3 in $(1 + ax)^4 = \binom{4}{3} a^3$
 $\binom{4}{3} a^3 = 1372$
 $4a^3 = 1372$
 $a = 7$

87. (D) modulus of $-1 + \sqrt{3}i$ is $\sqrt{(-1)^2 + (\sqrt{3})^2} = 2$
 and the argument is $\theta = \tan^{-1} \frac{\sqrt{3}}{-1} = \frac{2\pi}{3}$

88. (A) $x^2 - 10x + 17 = (x - 5)^2 - 8$
 So $a = 5$ and $b = -8$

89. (A) $|3x - 2| < 5$
 $-5 < 3x - 2 < 5$
 $-5 + 2 < 3x < 5 + 2$
 $-\frac{3}{3} < x < \frac{7}{3}$

90. (D) Common difference $d = \frac{y-x}{4}$
 $m_1 = x + \frac{y-x}{4} = \frac{3x+y}{4}$
 $m_2 = \frac{3x+y}{4} + \frac{y-x}{4} = \frac{x+y}{2}$
 $m_2 = \frac{x+y}{2} + \frac{y-x}{4} = \frac{x+3y}{4}$

91. (C) The function is of the form $\frac{0}{0}$ for $x = 0$
 For $x < 0$, $f(x) = -1$
 For $x > 0$, $f(x) = 1$
 So the range is $\{-1, 1\}$

92. (B) $\int \frac{1}{f(x)} dx = \log[f(x)]^2 + c$
 $\frac{1}{f(x)} = 2 \frac{1}{f(x)} f'(x)$
 $\frac{1}{2} = f'(x)$
 $f(x) = \frac{1}{2}x + k$

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93. (A) $x^2 - 4x - 12y - 32 = 0$
 $(x - 2)^2 = 12(y + 3),$
So vertex = (2, -3) and latus rectum = 12

94. (A) $xy + 2x - y - 2 = 0$
 $x(y + 2) - 1(y - 2) = 0$
 $(x - 1)(y + 2) = 0$
These pair of st. lines are parallel to x-axis and y-axis. So they are perpendicular to each other.

95. (C) $f(x) = x + \sin x$
 $f'(x) = 1 + \cos x$
 $f''(x) = -\sin x$
For max or min $f'(x) = 0$
 $1 + \cos x = 0$
 $x = \pi$
And $f''(x) = 0$. So neither max. nor min.

96. (A) Area bounded by $y = \ln x$, the x- axis and the straight line $x = e$

$$\int_1^e \ln x = [x \ln x - x]_1^e = e$$

97. (D) $y = ax^2 - 2x + b$ passes through (1,2)
so $2 = a - 2 + b$

$$a + b = 4$$

$\frac{dy}{dx} = 2ax - 2$ but the tangent is parallel to x axis at

$x = -1$, Therefore, $\frac{dy}{dx} = 0$ at $x = -1$

$-2a - 2 = 0$, so $a = -1$ and $b = 5$.

98. (D) $3\cos^{-1}x + \sin^{-1}x = \pi$

$$3\cos^{-1}x + \frac{\pi}{2} - \cos^{-1}x = \pi$$

$$2\cos^{-1}x = \frac{\pi}{2} \quad \text{so } x = \frac{1}{\sqrt{2}}$$

99. (B) 100. (B)
